

12 *Mr. Bellamy, Distribution of Stars Photographed LX. 1,*

observations made rather determine this photometric value than the amount of the magnitude-equation. Dr. Gill has begun measuring star photographs with a very accurate micrometer. I cannot help thinking that if he will take a few plates near the equator, and measure them for comparison with his meridian observations, he will quickly and easily determine the magnitude-equation and find reason to revise his opinion of the value of the "screen" method. In any case the independent check would be very valuable.

On the Distribution of Stars Photographed at the University Observatory, Oxford, for the Astrographic Catalogue for Zones +25° to +29°. By F. A. Bellamy.

In *The Observatory* for 1899 July the Astronomer Royal gave a table of the comparison of the number of stars in the Greenwich Astrographic Catalogue, zones +6° to +7°, with those in B.D. and in the A.G.C. (Helsingfor and Christiania). The total number of stars is given for each hour of R.A. (58,170 stars for the twenty-four hours), the number per square degree—the mean being 70°—the number in B.D. and in A.G.C., and the ratios to Greenwich measures; these ratios are 5.8 and 11.7 respectively. It should be remarked that all the plates had exposures of 6^m, 3^m, and 20^s; that all the plates not showing—with the shortest exposure—stars of the 9^o mag. on Argelander's scale were rejected; and, thirdly, by the method adopted for measurement, which avoids overlap of adjacent plates, no stars are counted more than once: that article suggested a similar discussion of the Oxford measures.

Firstly, for reasons which need not be entered into here,* the Oxford plates have not all been taken with the uniform exposures of 6^m, 3^m, and 20^s, but these only will be used in this discussion; secondly, the plates are not so consecutive or contiguous, though as numerous, as those used in forming the table for Greenwich; and, thirdly, the basis for the rejection of a plate was not the visibility of the ninth magnitude stars, but the criterion of having three times the number of stars counted within the same area on Argelander's charts, slight allowance being sometimes made if the plate had already been measured and the total number of stars came near the limit. Table I. shows that an average of 4^c times B.D. stars has been maintained, and 7.4 times the stars in the Cambridge Catalogue.

In spite of these differences the following table may be regarded as fairly comparable with that for Greenwich: the numbers for Greenwich are not repeated, but may be gathered from the Plate I accompanying this table.

* 23rd Report to the Board of Visitors, University Observatory, Oxford, p. 7.

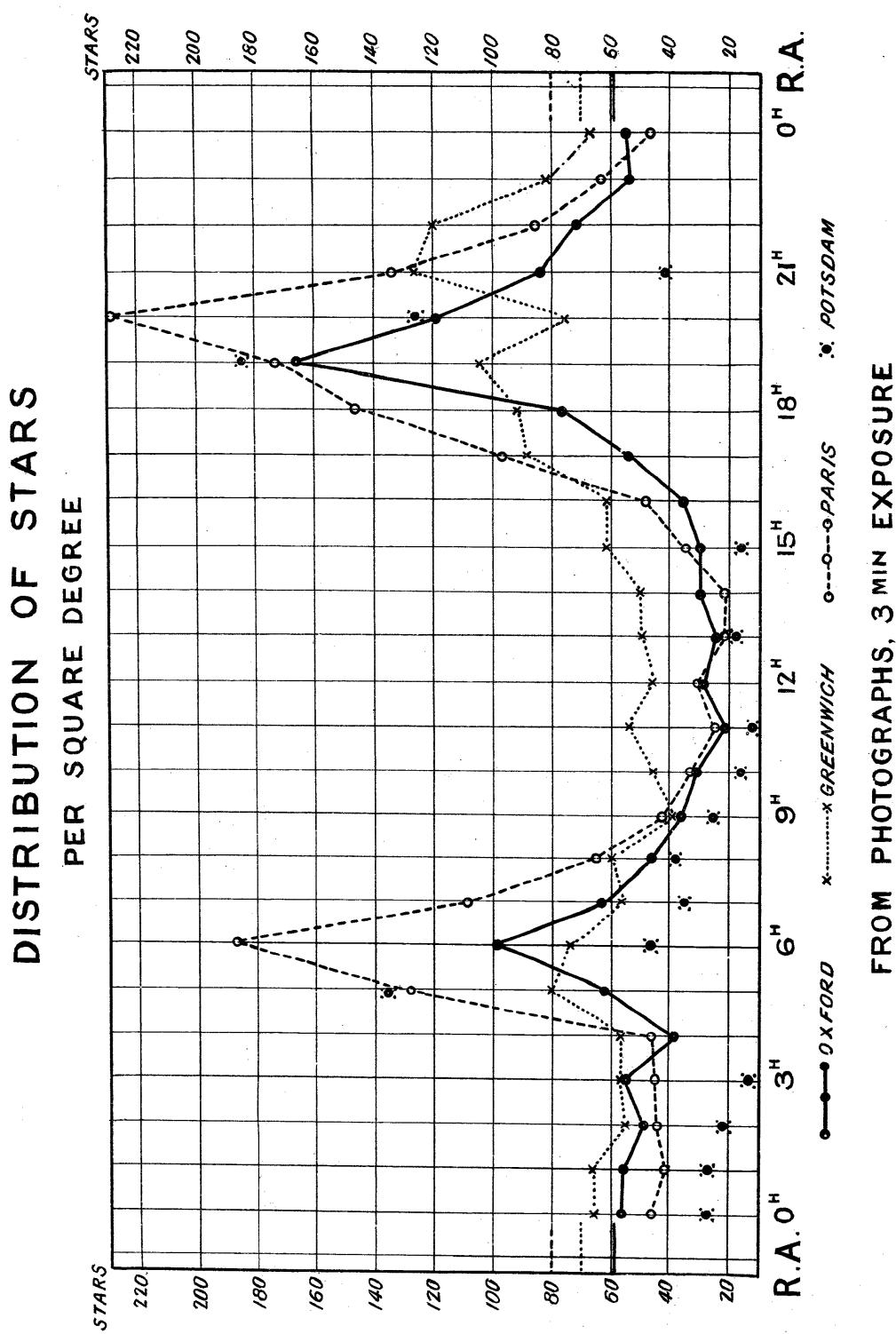


TABLE I.

Hour.	No. of plates,	Total stars measured.	Average No. of stars.	Stars in B.D.	Stars in B.D. to B.D.	Stars in same area.	Count, stars in same area.	Stars in same area.	Stars in same area.	Hour.
0	35	9283	265	56	4.6	4.6	1393	1393	6.9	0
1	28	7227	258	55	4.3	4.3	859	859	8.4	1
2	25	5784	231	49	4.8	4.8	690	690	8.4	2
3	21	5428	259	55	4.4	4.4	599	599	9.0	3
4	18	3224	179	38	4.4	4.4	328	328	9.8	4
5	23	6578	286	61	3.5	3.5	822	822	8.0	5
6	20	9322	466	99	3.7	3.7	988	988	9.4	6
7	23	6533	284	60	3.3	3.3	934	934	7.0	7
8	22	4751	216	46	3.4	3.4	683	683	7.0	8
9	25	4216	169	36	3.3	3.3	600	600	7.0	9
10	19	2733	144	31	3.1	3.1	499	499	5.5	10
11	12	1263	105	22	2.6	2.6	262	262	4.9	11
12	18	2407	134	29	3.2	3.2	422	422	5.7	12
13	23	2574	112	24	2.9	2.9	530	530	4.9	13
14	19	2718	143	30	3.4	3.4	449	449	6.0	14
15	12	1668	139	30	2.9	2.9	287	287	5.8	15
16	13	2208	170	36	3.0	3.0	403	403	5.5	16
17	12	3024	252	54	3.3	3.3	478	478	6.3	17
18	16	5764	360	77	3.7	3.7	901	901	6.4	18
19	17	13189	776	165	6.3	6.3	1239	1239	10.6	19
20	23	12877	560	119	4.7	4.7	1754	1754	7.4	20
21	27	10673	395	84	4.4	4.4	1686	1686	6.3	21
22	29	9768	337	72	4.4	4.4	1165	1165	8.4	22
23	33	8327	252	54	4.0	4.0	1097	1097	7.6	23
Sums	513	141539	...	35148	...	19068	
Weighted means			276	58.7	...	4.0	...	7.4	...	

From an inspection of the Greenwich curve in Plate I a very prominent maximum stands out at 21^h and 22^h, but that at 5^h and 6^h is less pronounced; in fact, the distribution throughout the twenty-four hours is relatively more uniform, and is maintained at a higher ratio per square degree than in the Oxford zones, where two marked maxima occur at 6^h and 19^h, and a rather definite minimum at 11^h-13^h. While the Greenwich mean density is 70.0 stars per square degree, that at Oxford is 58.7 stars.

The proximity of the Greenwich zones to the Milky Way is

in fact more continuous than that of the Oxford zones, which cut the Milky Way almost at right angles, at R.A. $5^h 30^m$ to $7^h 15^m$, and at 17^h to 21^h , whilst the Greenwich plates are actually in it from R.A. 19^h to about 5^h .

I have also collected information from the Paris Observatory Reports for 1893-97 for the Paris zones, which are contiguous to the Oxford zones on the southern side, and for the Potsdam zones * on the northern side; the results are exhibited in Table II., and included in Plate I.

TABLE II.
Average numbers of stars measured on plates.

Hour.	Paris.			Stars per sq. deg.	Potsdam.	
	Zone +22°. Stars.	Zone +23°. Stars.	Zone +24°. Stars.		Zones +32° to +33°. Stars.	Stars per sq. deg.
0	202 ₈	254 ₇	192 ₄	47	124 ₃	26
1	132 ₇	238 ₈	244 ₁	41	127 ₃	27
2	275 ₆	195 ₇	170 ₈	44	110 ₁	21
3	324 ₂	171 ₈	234 ₅	45	63 ₁	13
4	...	278 ₆	176 ₈	47
5	593 ₅	735 ₈	448 ₇	127	629 ₁₈	134
6	780 ₇	1066 ₇	788 ₈	187	216 ₂	46
7	427 ₇	629 ₇	451 ₇	107	166 ₄	35
8	369 ₆	339 ₆	196 ₆	64	177 ₇	38
9	200 ₃	211 ₇	162 ₆	41	117 ₁	25
10	...	137 ₇	179 ₃	32	73 ₃	16
11	...	129 ₇	116 ₇	26	57 ₃	12
12	176 ₇	118 ₅	126 ₈	30
13	112 ₅	97 ₇	167 ₇	27	82 ₁	18
14	114 ₃	121 ₅	130 ₈	26
15	221 ₇	113 ₆	161 ₇	36	73 ₁	16
16	209 ₇	246 ₇	239 ₇	49
17	277 ₄	421 ₈	618 ₆	97
18	...	717 ₆	582 ₂	146	412 ₂	88
19	...	766 ₈	844 ₇	171	866 ₃	184
20	1145 ₅	1161 ₇	929 ₇	228	589 ₃	125
21	552 ₆	667 ₇	645 ₇	133	193 ₁	41
22	488 ₃	367 ₆	401 ₈	86
23	121 ₁	278 ₇	333 ₇	62

The number of plates is given after each quantity.

* *Publicationen des Astrophysikalischen Observatoriums zu Potsdam, Photographische Himmelskarte, Band I. xxviii.*

The Paris plates yield results in close agreement with those of Oxford, except that the two maxima—in the Milky Way—are more pronounced, and in consequence the mean number of stars per square degree (80.4) is even higher than that for Greenwich (70.0). With reference to this point it may be remarked that the two maxima in the Oxford curve are reduced in magnitude by the omission of a number of plates in the Milky Way which received exposures different from 6^m, 3^m, 20^s, and by the inclusion of some old plates which in this rich region contained enough stars for the purposes of the Astrographic Catalogue, though in a poorer region similar plates have been rejected.

To examine the influence of galactic latitude on such numbers the galactic latitudes of the hourly groups, both for Oxford and Greenwich, were read from a globe. The mean declination of the Oxford zones has been taken, 28° (probably +27° would be a more correct mean of the plates actually used in this paper), and the pole of the galaxy as 12^h 41^m 20^s + 27° 21'*: these readings are given in Table III. column (2). Column (3) shows the actual mean number of stars measured, as in Table I. or in the Greenwich Table; these two quantities were then taken as arguments, and a curve (Plate 2, diagrams 1 and 2) drawn through the points plotted for each hour of R.A., the ordinates (column 4) were then read from this curve and compared with column (3), and a difference (Oxford or Greenwich *minus* Oxford Curve) formed (column 5); the percentage of deviation is given in column (6).

TABLE III.

Oxford.

R.A.	Galactic Latitude.	No. of Stars.	Curve.	Obsn. Minus Curve.	Percentage.	R.A.	Galactic Latitude.	No. of Stars.	Curve.	Obsn. Minus Curve.	Percentage.
0 ^h 35 ^o	+ 35	265	200	+ 65	+ 24	12 ^h 2 ^m	- 88 ^o	134	115	+ 19	+ 15
1 ^h 34 ^o	+ 34	258	205	+ 53	+ 20	13 ^h 2 ^m	- 80	112	115	- 3	- 3
2 ^h 29 ^o	+ 29	231	230	+ 1	0	14 ^h 2 ^m	- 66	143	125	+ 18	+ 12
3 ^h 21 ^o	+ 21	259	290	- 31	- 12	15 ^h 2 ^m	- 53	139	140	- 1	0
4 ^h 13 ^o	+ 13	179	410	- 231	- 129	16 ^h 2 ^m	- 40	170	170	0	0
5 ^h 1 ^o	+ 1	286	740	- 454	- 159	17 ^h 2 ^m	- 27	252	250	+ 2	+ 1
6 ^h 10 ^o	- 10	466	470	- 4	- 1	18 ^h 2 ^m	- 14	360	385	- 25	- 7
7 ^h 22 ^o	- 22	284	285	- 1	0	19 ^h 2 ^m	- 2	776	725	+ 51	+ 7
8 ^h 35 ^o	- 35	216	200	+ 16	+ 7	20 ^h 2 ^m	+ 8	560	505	+ 55	+ 10
9 ^h 48 ^o	- 48	169	150	+ 19	+ 11	21 ^h 2 ^m	+ 18	395	320	+ 75	+ 19
10 ^h 61 ^o	- 61	144	130	+ 14	+ 10	22 ^h 2 ^m	+ 25	337	265	+ 72	+ 21
11 ^h 74 ^o	- 74	105	120	- 15	- 14	23 ^h 2 ^m	+ 33	252	200	+ 52	+ 20
(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)

* *Uranometria Argentina*, Gould, p. 370.

TABLE III—continued.

Greenwich.

R.A.	Galactic Latitude.	No. of Stars.	Curve.	Obsn. Minus Curve.	Per-centage.	R.A.	Galactic Latitude.	No. of Stars.	Curve.	Obsn. Minus Curve.	Per-centage.
0 ^h	+ 4°	305	630	- 325	- 108	12 ^h 1/2	+ 49°	218	150	+ 68	+ 3
1 ^h 1/2	+ 5	310	600	- 290	- 94	13 ^h 1/2	+ 48	231	150	+ 81	+ 3
2 ^h 1/2	+ 6	261	585	- 324	- 124	14 ^h 1/2	+ 46	236	155	+ 81	+ 3
3 ^h 1/2	+ 10	260	480	- 220	- 85	15 ^h 1/2	+ 42	289	175	+ 114	+ 3
4 ^h 1/2	+ 14	262	390	- 128	- 41	16 ^h 1/2	+ 37	283	195	+ 88	+ 3
5 ^h 1/2	+ 18	377	315	+ 62	+ 16	17 ^h 1/2	+ 31	414	225	+ 189	+ 7
6 ^h 1/2	+ 24	343	275	+ 68	+ 20	18 ^h 1/2	+ 25	433	270	+ 163	+ 3
7 ^h 1/2	+ 30	264	230	+ 34	+ 13	19 ^h 1/2	+ 20	486	315	+ 171	+ 3
8 ^h 1/2	+ 35	271	200	+ 71	+ 26	20 ^h 1/2	+ 15	356	385	- 29	-
9 ^h 1/2	+ 40	184	184	0	0	21 ^h 1/2	+ 10	594	475	+ 119	+ 2
10 ^h 1/2	+ 44	217	160	+ 57	+ 26	22 ^h 1/2	+ 7	564	564	0	
11 ^h 1/2	+ 48	247	150	+ 97	+ 29	23 ^h 1/2	+ 5	378	600	- 222	- 5
(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)

For Oxford the agreement is good ; but there are two exceptional hours, $4\frac{1}{2}^h$ and $5\frac{1}{2}^h$, which cannot be brought within reasonable agreement without throwing out a considerable portion of the curve. But it is at once obvious that neither this Oxford curve, which has been used for Greenwich differences in Table III., nor any other curve, will suit the results from the Greenwich plates ; in other words the number of stars on a plate does not vary simply as any function of the galactic latitude. This indeed appears from the B.D. To bring out the facts clearly the following information was obtained.

The number of stars per square degree was formed from the stars in B.D. for every tenth degree and for each hour.

The points were plotted and curves drawn ; these curves were used as a basis for forming diagram 3 (Plate 2).

To show more clearly the relation of the curves of equal density to the galaxy, I have made diagram 4 (Plate 2) where the abscissæ represent galactic longitudes and the ordinates galactic N.P.D.

It can be seen that the Oxford zones pass through the minimum area of star distribution (according to the stars given in the B.D.), and are within a region containing an average of less than 12 stars per square degree from R.A. $8\frac{1}{2}^h$ to 16^h , also again from 0^h to 3^h ; in fact more than half the Oxford zones. On the contrary, they almost cut the Milky Way at right angles at $5^h 30^m$, and leave it at $6\frac{3}{4}^h$ or 7^h , and again enter at $17\frac{1}{2}^h$ and remain within it till nearly 22^h . The reason of the less variation between the Greenwich maxima and minimum is also apparent, but the fall at 20^h is unexplained. It must be

Diagram 1.

OXFORD

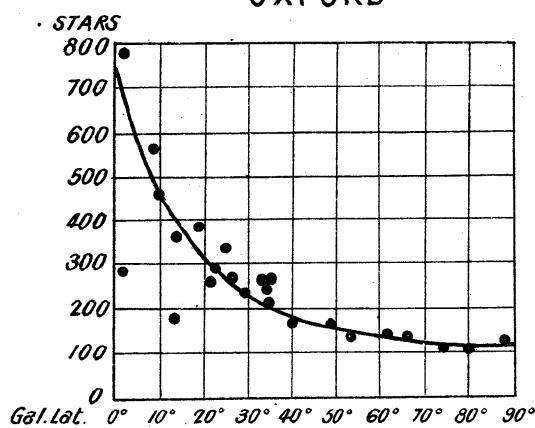


Diagram 2.

GREENWICH.

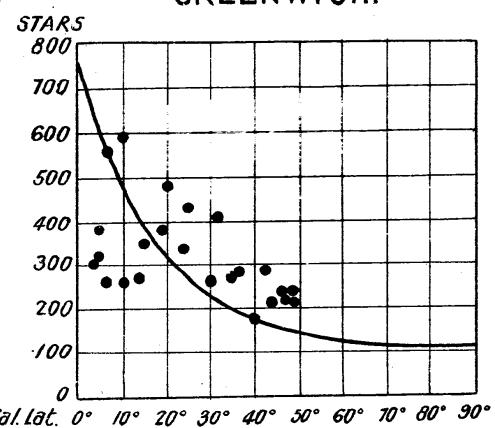
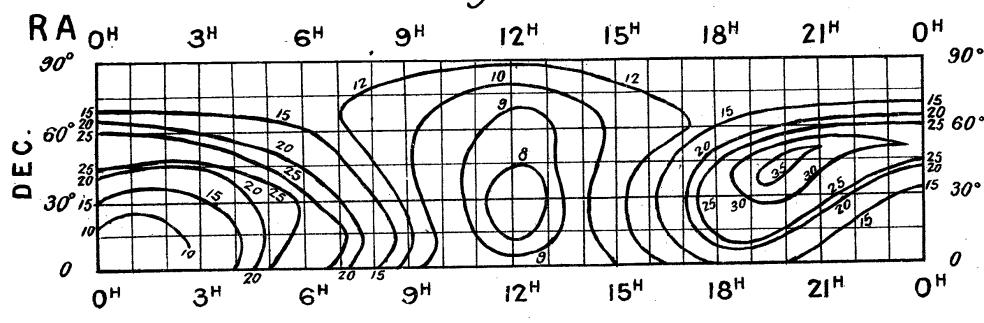


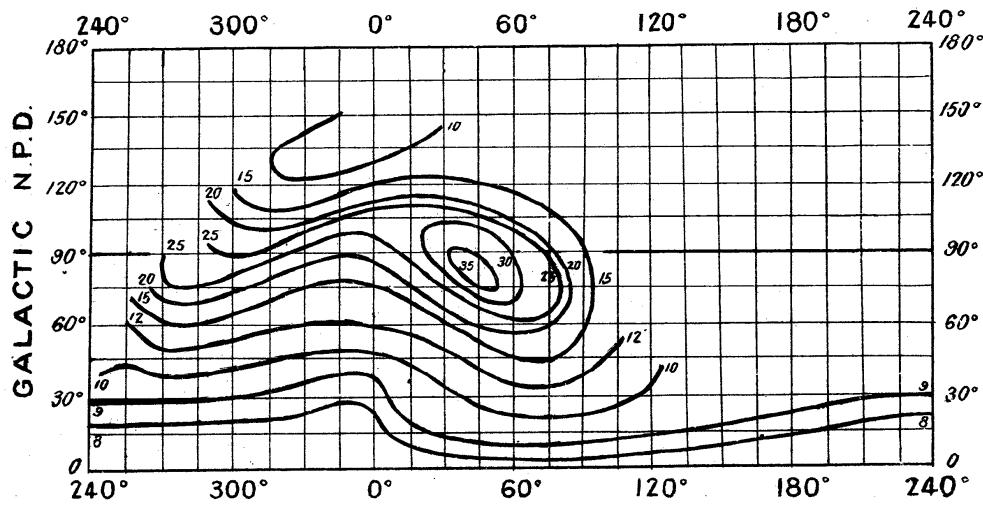
Diagram 3.



EQUAL DENSITY LINES FOR B.D. STARS

Diagram 4.

GALACTIC LONGITUDE



Nov. 1899. *Messrs. Dyson and Hollis, Diameters of Images etc.* 17

remembered that in comparing Plate 1 and Plate 2, diagram 3, the comparison is one between density from B.D. stars (to the $9\frac{1}{2}$ mag.) and from photographs giving stars as low as the $10\frac{1}{2}$ and 11 magnitudes.

When all the zones are completed it will be interesting to form a similar set of curves of equal density for stars to the 11th magnitude shown on the photographs and compare them with these found from Argelander's eye observations.

Comparison of the Diameters of the Images of Stars on the Greenwich Astrographic Plates with the Magnitudes given in the 'Bonn Durchmusterung.' By F. W. Dyson, M.A., and H. P. Hollis, B.A.

§ 1. This paper consists of a comparison of the diameters of the images on 232 astrographic plates with the magnitudes of the stars as given in the *Bonn Durchmusterung*. The number of stars contained in the *B. D.* varies from about 20 to 100 per plate, so that the diameters of more than 10,000 images have been considered. The object of the paper is not to obtain a formula connecting diameter and magnitude from any physical considerations, but rather to tabulate observations, to see what changes there are from plate to plate, and to test the uniformity of Argelander's scale.

The photographs considered are those whose centres are at dec. $+65^\circ$, $+66^\circ$, and $+67^\circ$. They were taken at various times between 1892 April and 1898 March. The images whose diameters have been measured twice in the regular measurement of the Greenwich plates had an exposure of 6^m. The plates used were "Ilford Special Rapid," "Mawson," and "Rocket."

The diameters of the images are measured in units of $0''\cdot3$ or $\frac{1}{100}$ th of one réseau interval by each of the measurers, and the sum of the measures is given, so that the measures of diameter are expressed in units of $0''\cdot15$. Measurement of the diameters of the photographic images of stars are necessarily somewhat arbitrary, especially at some distance from the centre of the field, when the images are elongated and faint. The measurers were instructed to make some allowance for this, the general principle being to give the diameter the stars would have had if near the centre of the plate.

§ 2. The diameters of all the stars contained in the *B. D.* were tabulated for each plate. Plate 1548, the first plate in zone 67° , may be given as a specimen.

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